

CS 856: Programmable Networks

Lecture 7: Network Verification

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Winter 2024

Logistics

- Project progress report is due **Sunday, March 10th**
 - Two pages
 - Briefly describe the motivation and problem statement
 - Briefly describe the related work, including any new ones you have found since the proposal
 - Describe what you have achieved so far
 - Describe what you plan to do for the rest of the term
- Assignment 2 will be released next week and is optional (extra credit)

Formal Verification

Proving or disproving
the **correctness** of a (software or hardware) system
with respect to a certain **formal specification or property**
using formal methods of mathematics

Formal Verification



e.g., Traffic light controller

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**Safety properties:
nothing bad happens**

e.g., traffic light should not be
simultaneously green in both direction

Formal Verification

e.g., Traffic light controller

Proving or disproving

the **correctness** of a (software or hardware) system

with respect to a certain **formal specification or property**

using formal methods of mathematics

Safety properties:
nothing bad happens

e.g., traffic light should not be
simultaneously green in both direction

Liveness properties:
something good eventually happens

e.g., If there is a car on the road, the light
will eventually turn green

Formal Verification

Proving or
the **correctness** of a (soft
with respect to a certain **formal specification or property**
using formal methods of mathematics

Broadly applicable!

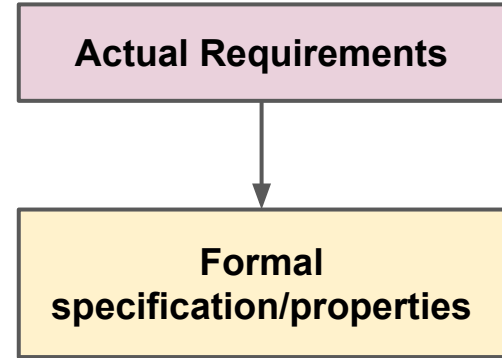
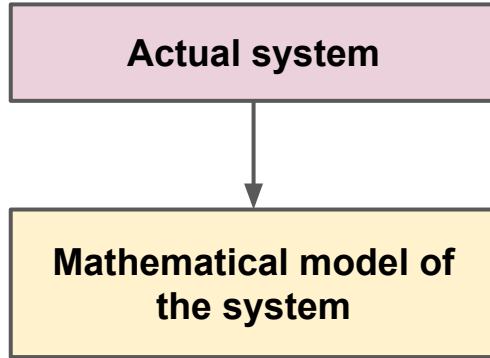
- Hardware design
- Software
- Distributed systems
- **Computer Networks**
- Aviation
- Neural Networks
- ...

How do we go about verifying a system?

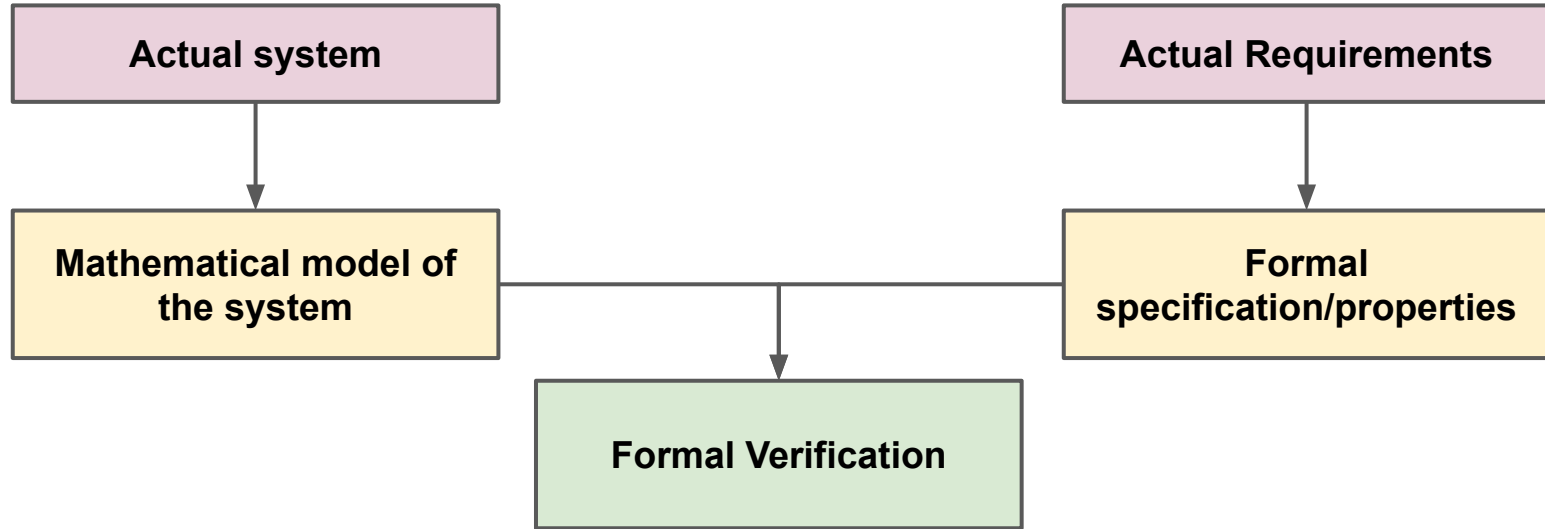
Actual system

Actual Requirements

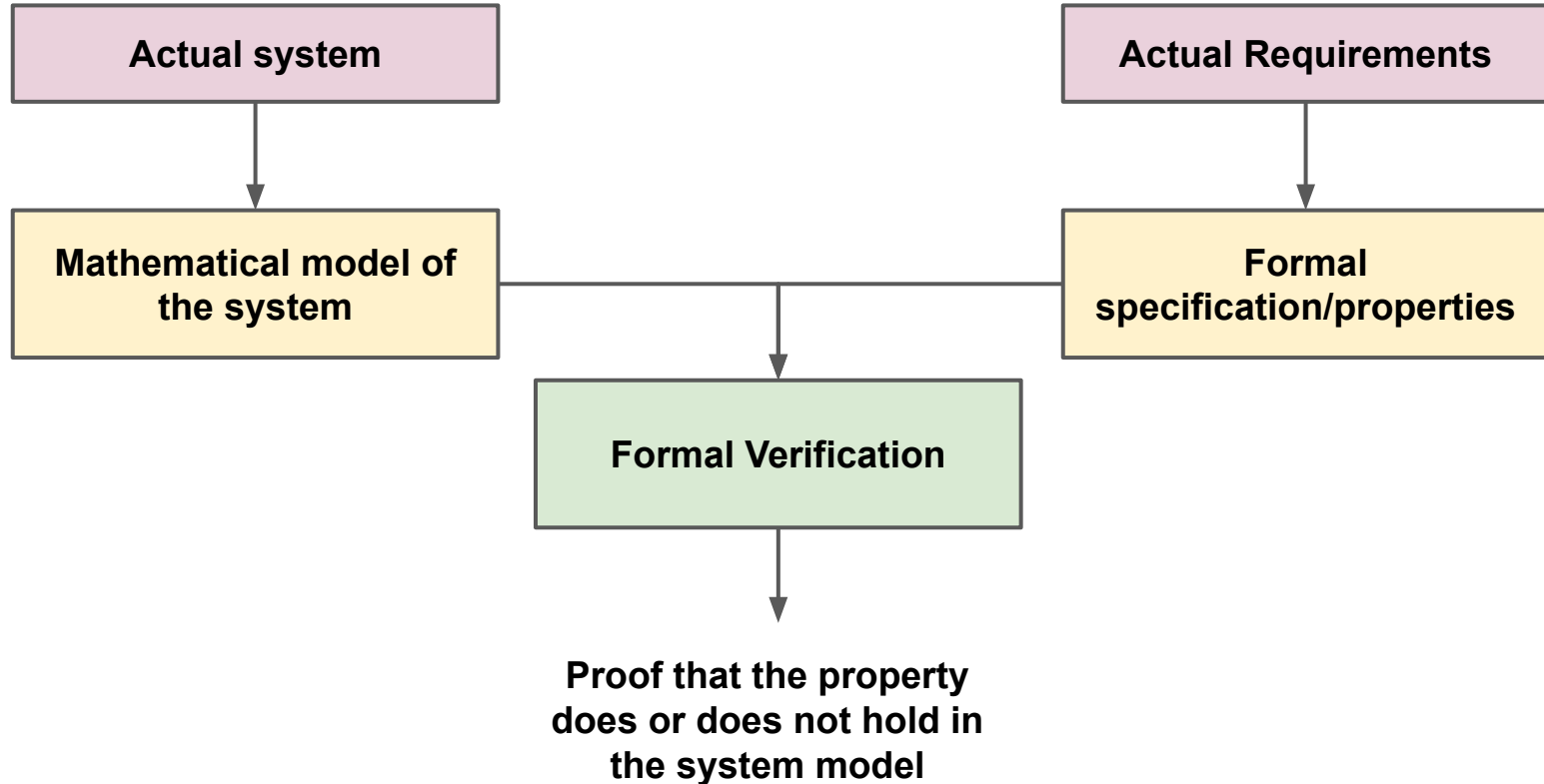
How do we go about verifying a system?



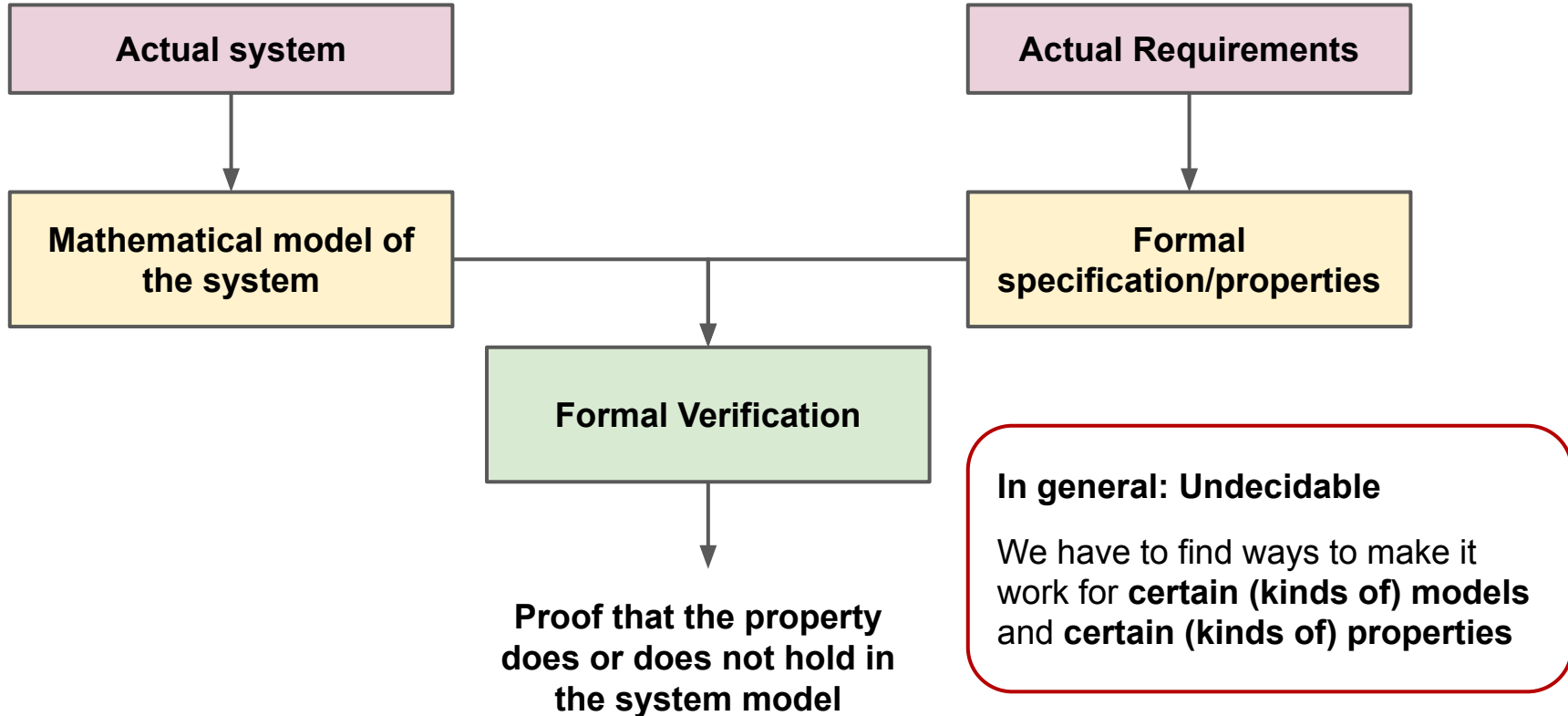
How do we go about verifying a system?



How do we go about verifying a system?



How do we go about verifying a system?



A (very) simple example

The following example is adapted from Aarti Gupta's Fall'15 course on "Automated Reasoning about Software" at Princeton University

A (very) simple example

```
bool x;  
int y = 8;  
int z = 0;  
int w = 0;  
if (x)  
    z = y - 1  
else  
    w = y + 1  
  
assert(z == 5  
|| w == 9)
```

A (very) simple example

Actual program

```
bool x;  
int y = 8;  
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assert(z == 5  
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Actual requirements

A (very) simple example

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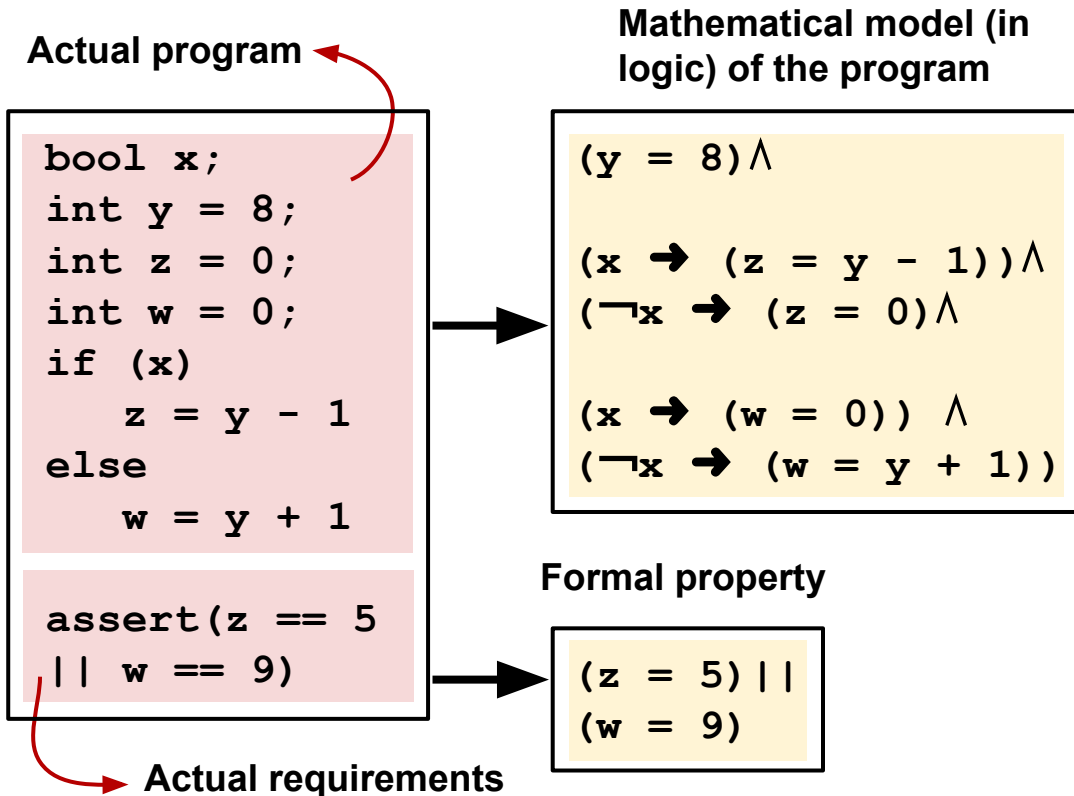
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assert(z == 5  
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```

Actual requirements

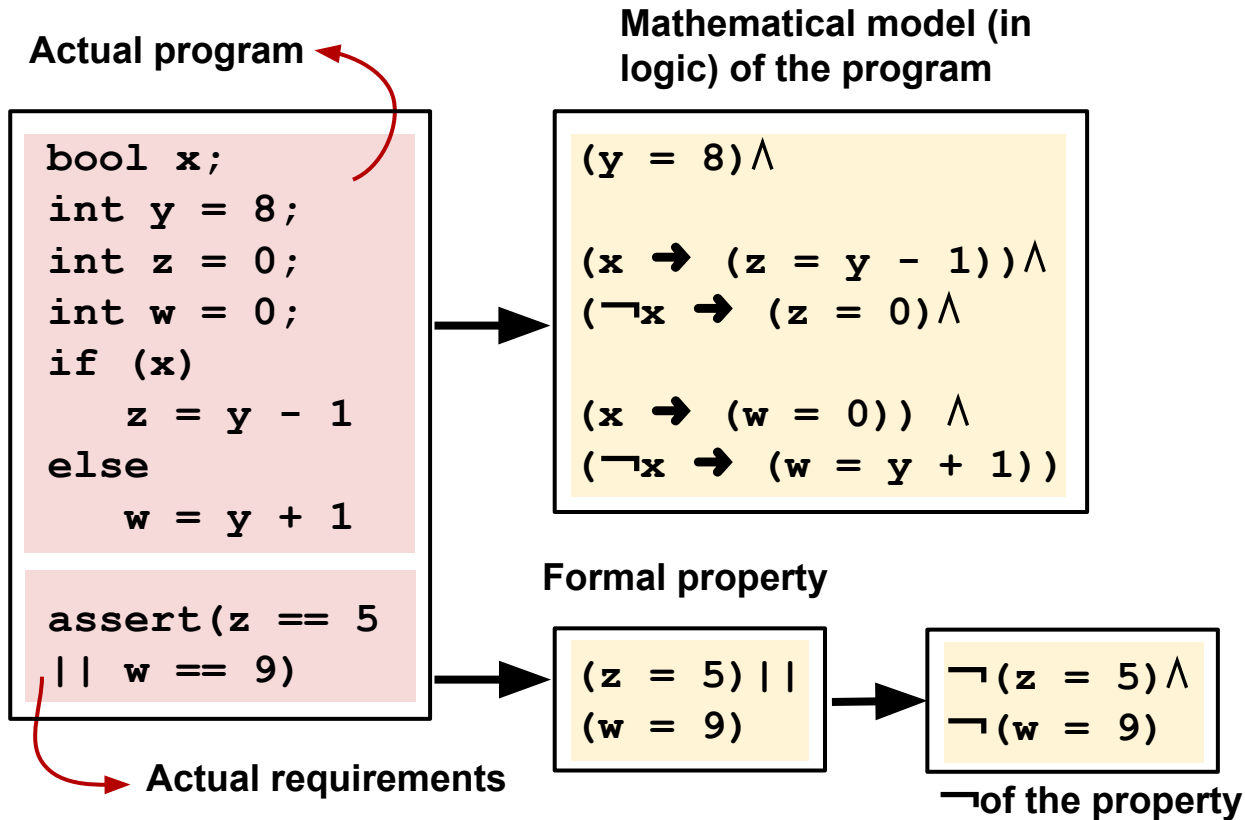
Mathematical model (in logic) of the program

```
(y = 8) ∧  
(x → (z = y - 1)) ∧  
(¬x → (z = 0)) ∧  
(x → (w = 0)) ∧  
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```

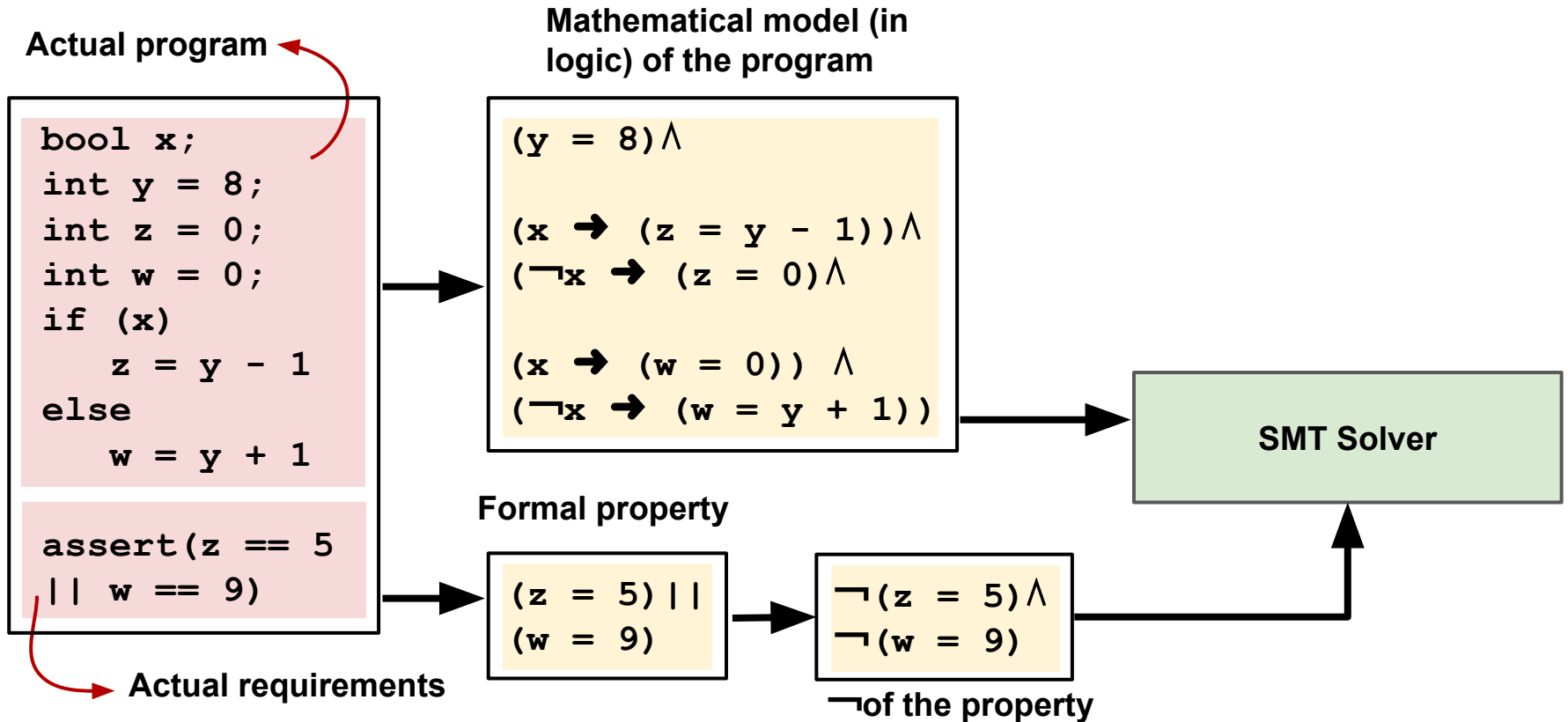

A (very) simple example



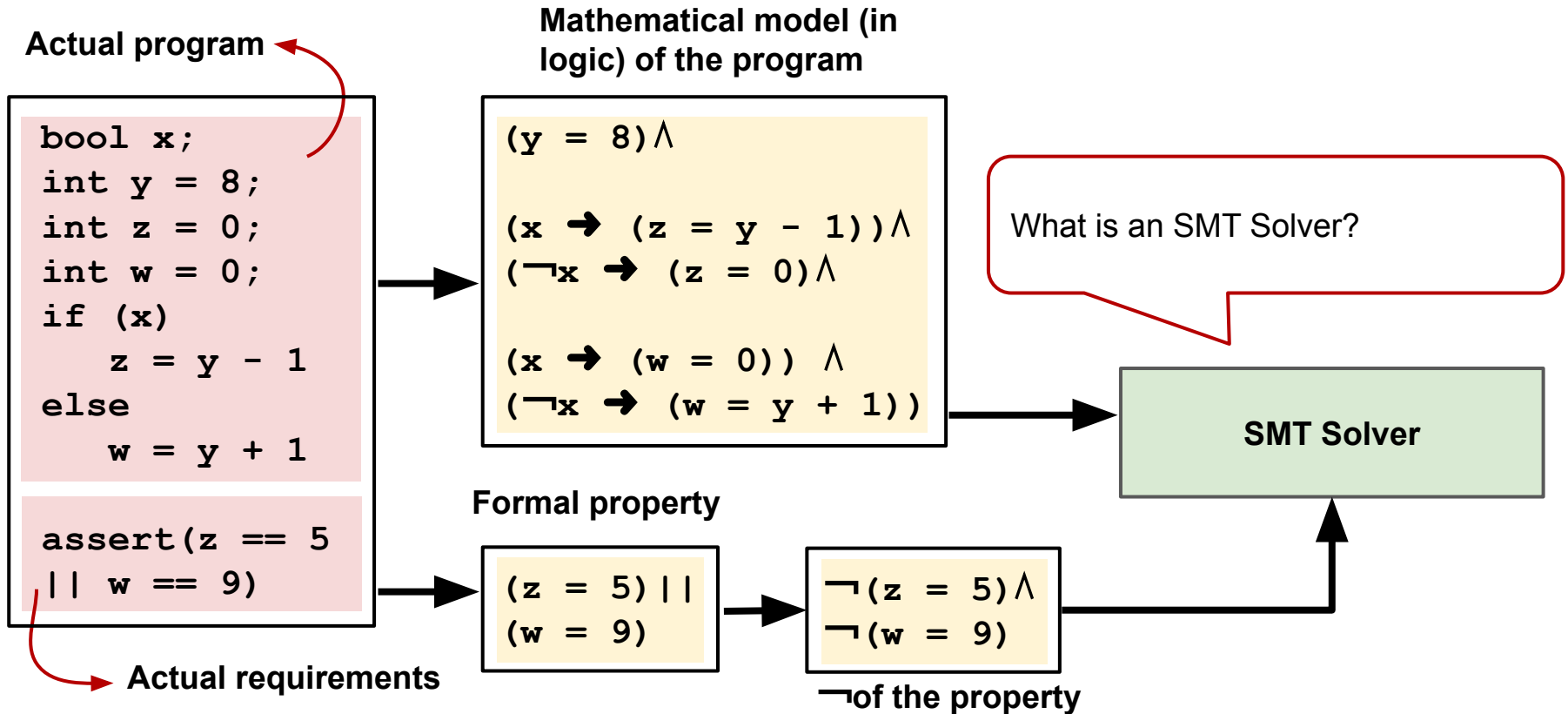
A (very) simple example



A (very) simple example



A (very) simple example



Satisfiability Modulo Theories (SMT)

- Let's look at the boolean satisfiability problem (SAT) first.

The (Boolean) Satisfiability Problem (SAT)

- Suppose you have a boolean formula
 - e.g., $(a \vee b) \wedge (\neg b \vee c)$
- You can assign true or false to each variable
- Is there an assignment that will make the entire formula evaluate to true?
- This is the SAT problem
- In general, it is NP complete
 - Unless $P = NP$, it can't be solved in polynomial time

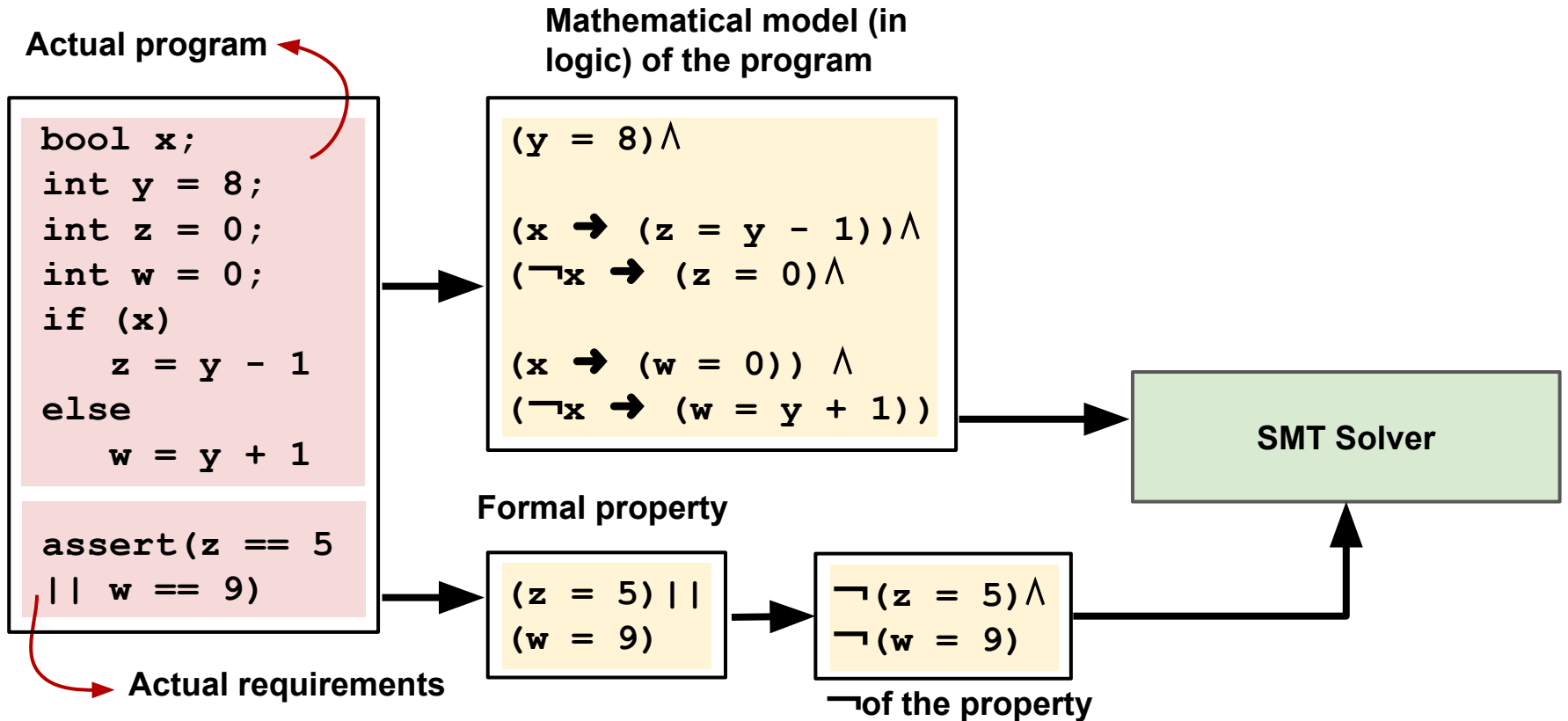
The (Boolean) Satisfiability Problem (SAT)

- The SAT problem, in general, is NP complete
 - Unless $P = NP$, it can't be solved in polynomial time
- Still, in the formal methods community, there has been a significant progress in tools that can, in many cases, solve this problem quite quickly for large formulas.

Satisfiability Modulo Theories (SMT)

- The same satisfiability problem, but for more complex (first-order-logic) formulas
 - integer variables, real variables, ...
 - arrays, bit vectors, lists, strings, ...
 - functions such as equality, addition, subtraction, ...
- Harder problem
 - can be NP-hard or undecidable depending on the "theory"
- but we have found ways to make it work by finding algorithms for analyzing certain families of formulas ("theories").

A (very) simple example



A (very) simple example

Actual program

```
bool x;  
int y = 8;  
int z = 0;  
int w = 0;  
if (x)  
    z = y - 1  
else  
    w = y + 1
```

```
assert(z == 5  
|| w == 9)
```

Actual requirements

Mathematical model (in logic) of the program

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(y = 8) ∧  
(x → (z = y - 1)) ∧  
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(x → (w = 0)) ∧  
(¬x → (w = y + 1))
```

Formal property

```
(z = 5) ||  
(w = 9)
```

```
¬(z = 5) ∧  
¬(w = 9)
```

¬of the property

Would any assignment to the variables x, y, z, and w make the following formula evaluate to true (Is it satisfiable)?

$model \wedge \neg property$

Yes!

$x = true, y = 8,$
 $z = 7, w = 0$

SMT Solver

A (very) simple example

Actual program

```
bool x;  
int y = 8;  
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(z = 5) ||  
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¬(z = 5) ∧  
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```

¬ of the property

`model ∧ ¬property`
evaluates to true for `x = true`,
`y = 8`, `z = 7`, `w = 0`

`model` evaluates to true → these
are a valid set of values for the
variables at the assertion location

`property` evaluates to false →
the assertion fails

SMT Solver

A (very) simple example

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Formal property

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(z = 5) ||  
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¬(z = 5) ∧  
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¬of the property

model $\wedge \neg$ property
evaluates to true for $x = \text{true}$,
 $y = 8$, $z = 7$, $w = 0$

Proves that the property does not hold with a counter-example

SMT Solver

A (very) simple example

Actual program

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A (very) simple example

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assert(z == 5  
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Let's change this to 7

Actual requirements

A (very) simple example

Actual program

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Actual requirements

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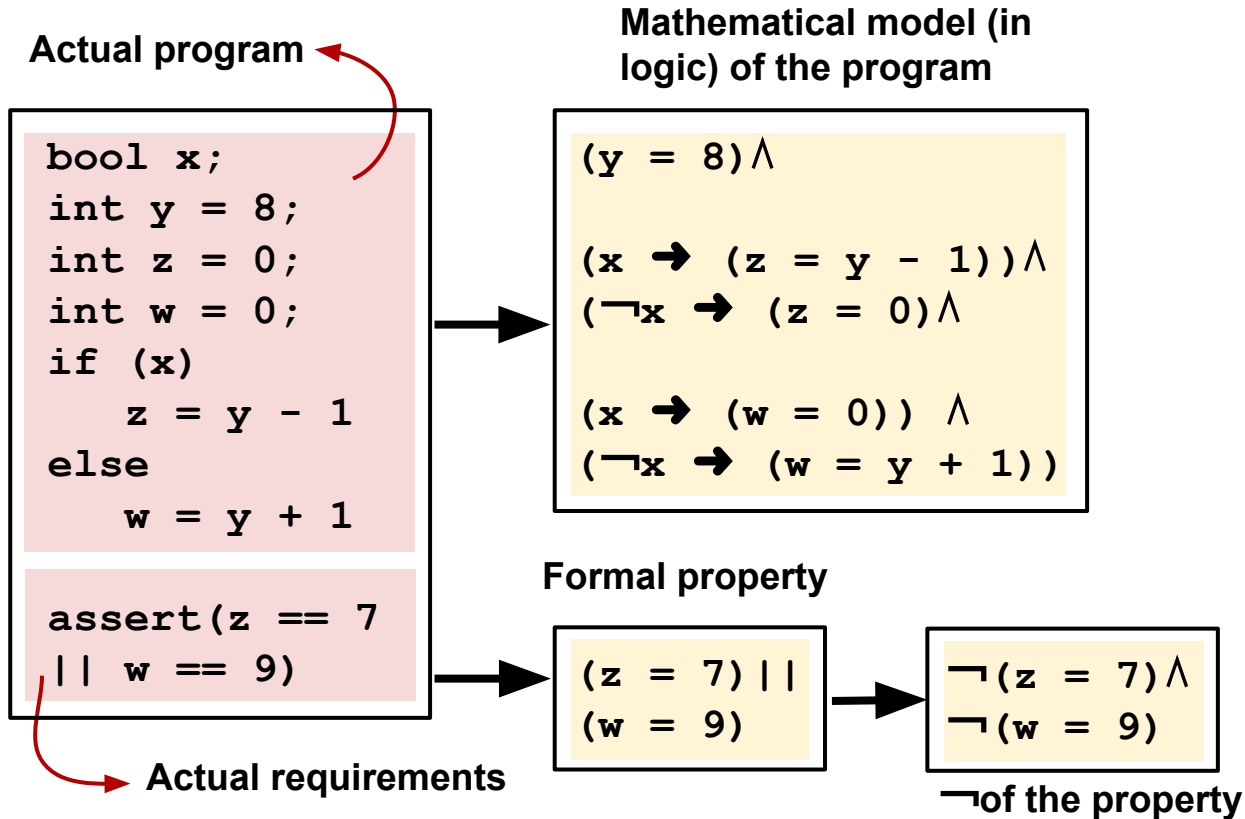
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```

Formal property

```
(z = 7) ||  
(w = 9)
```

```
¬(z = 7) ∧  
¬(w = 9)
```

¬of the property

SMT Solver

model $\wedge \neg$ property is not satisfiable!

Generates proof that there are no assignments to variables such that **model** evaluates to true and **property** evaluates to false.

We have proven that the program satisfies the property.

What we haven't talked about (and won't) in this lecture ...

- Kripke structures
- Temporal logic
- model checking
- symbolic execution
- Binary Decision Diagrams (BDD)
- Synthesis
- ...

What we haven't talked about (and won't) in this lecture ...

- Kripke structures
- Temporal logic
- model checking
- symbolic execution
- Binary Decision Diagrams
- **Synthesis**
- ...

Generating a "program" that satisfies a high-level formal specification

- Program synthesis
- Invariant synthesis
- compiler optimizations
- ...

Many use cases networking to generate:

- packet processing code for programmable data planes
- configurations and configuration updates
- control-plane repairs
- ...

Why use formal verification in networking?

- Networks are growing increasingly complex.
 - They can have hundreds or thousands of interacting components
 - The functionality running in each component is getting more complex
 - configurations files can grow as large as thousands of lines
- Networks are becoming a critical infrastructure
 - Bugs can take down the network or reduce its performance.
 - Network problems can affect thousands if not millions of people
- We need to catch bugs (or prove lack thereof) proactively before going into production

Formal verification in networking

- Started with verifying the forwarding properties of the data plane and control plane.
- Now expanding into more complex functionalities and properties
 - DNS, network performance, ...

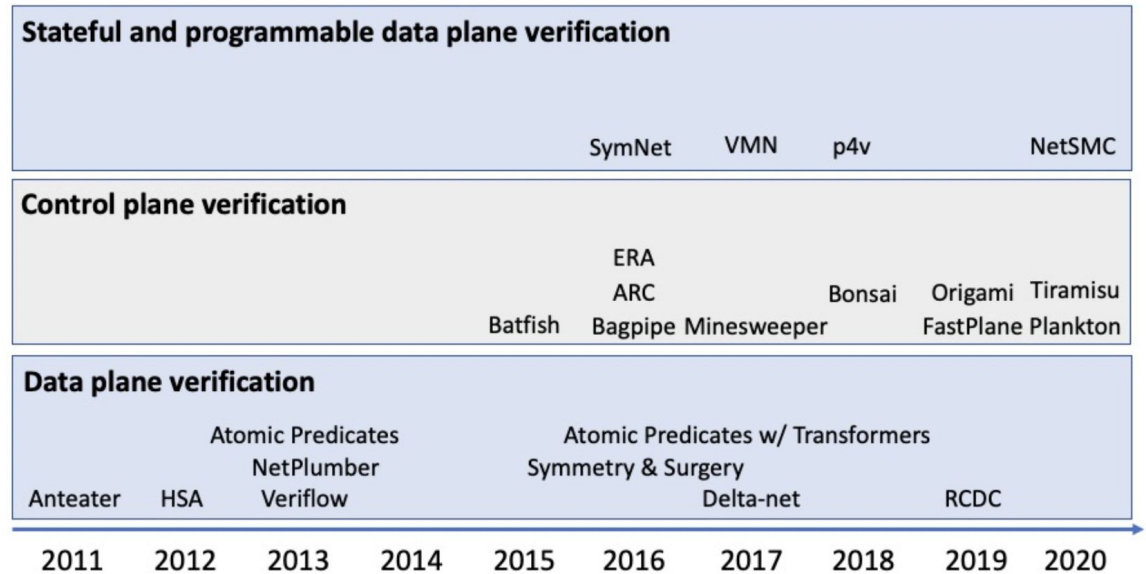


Figure taken from netverify.fun

Formal verification in networking

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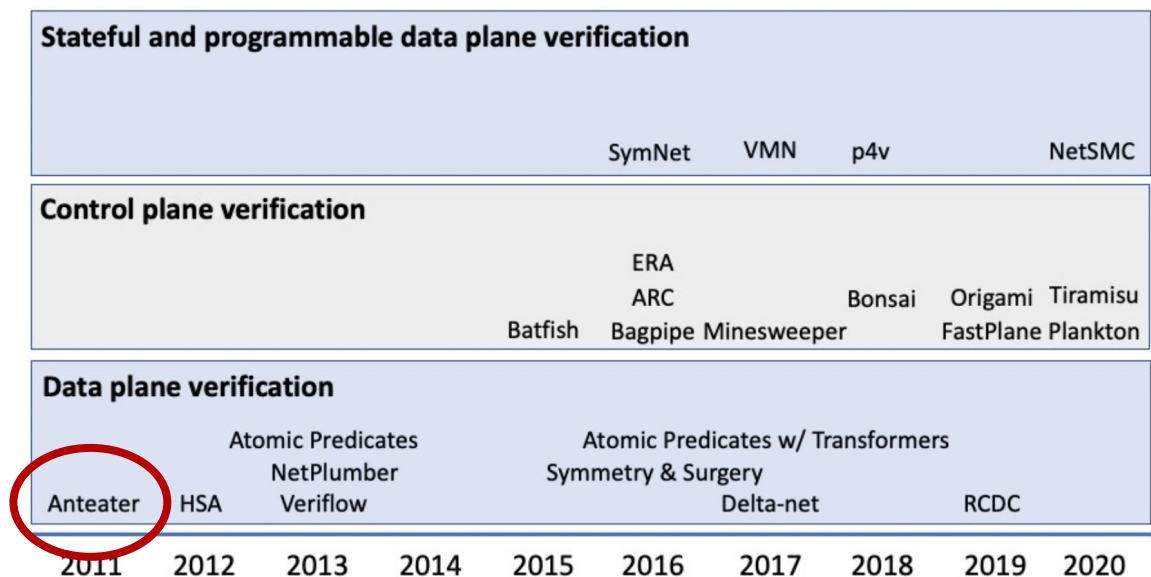
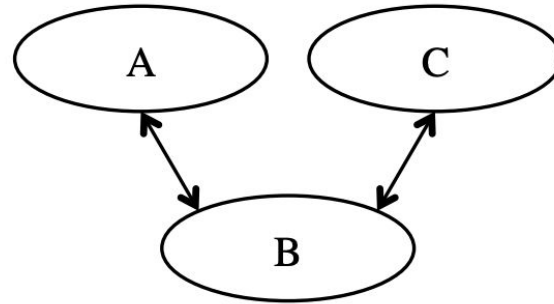


Figure taken from netverify.fun

Example - Anteater (SIGCOMM'11)

- Models the forwarding rule on the data plane as boolean formulas
- Uses a SAT solver to verify invariants about the network behavior
- The invariants are mostly related to forwarding
 - Reachability
 - Absence of forwarding loops
 - Absence of blackholes

Example - Anteater (SIGCOMM'11)



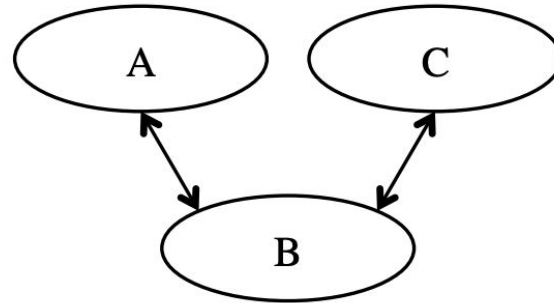
Example - Anteater (SIGCOMM'11)

A:

10.1.1.0/24 -> DIRECT

10.1.2.0/24 -> B

10.1.3.0/24 -> B



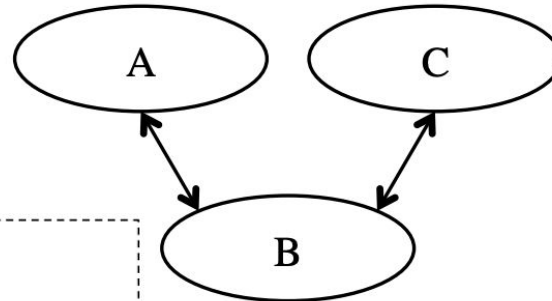
Example - Anteater (SIGCOMM'11)

A:

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B:

10.1.1.0/24 -> A

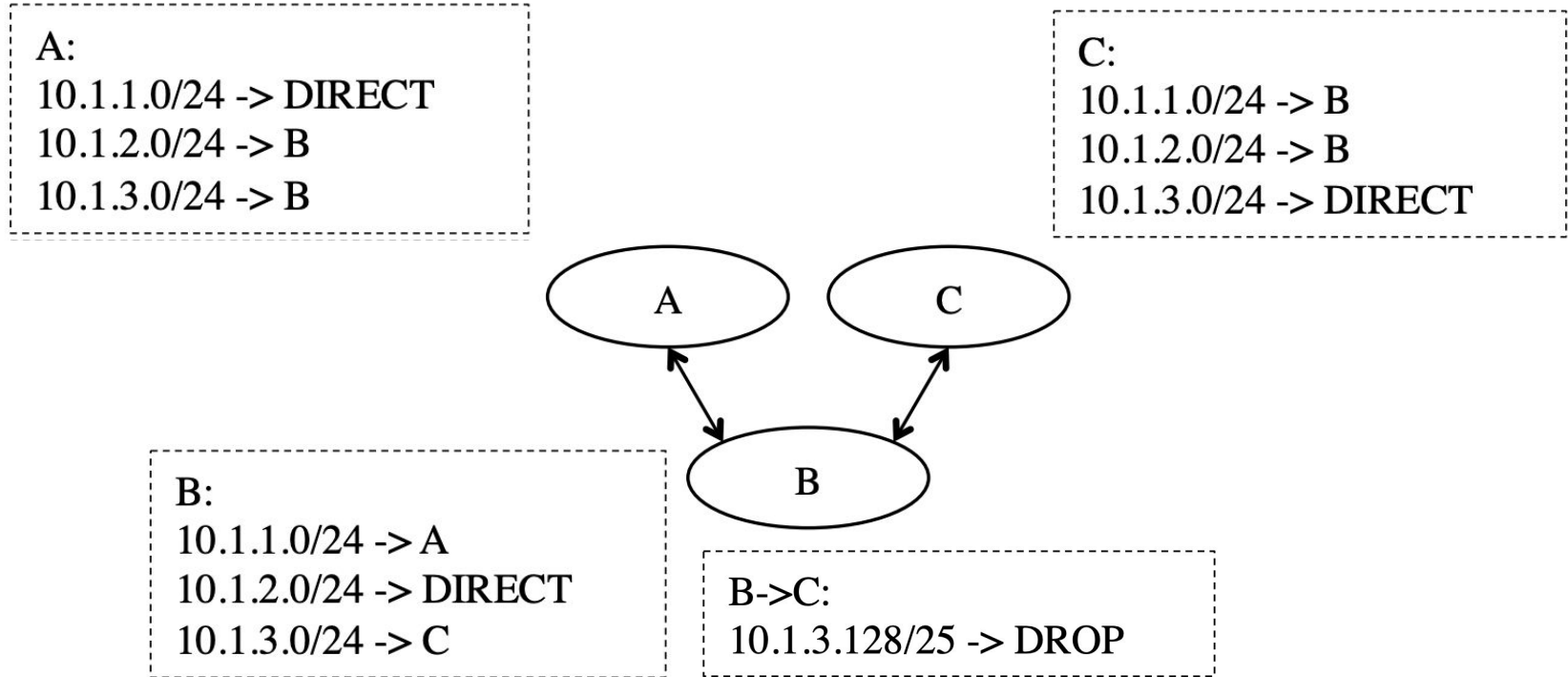
10.1.2.0/24 -> DIRECT

10.1.3.0/24 -> C

B->C:

10.1.3.128/25 -> DROP

Example - Anteater (SIGCOMM'11)



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10.1.3.0/24 -> B

B:

10.1.1.0/24 -> A

10.1.2.0/24 -> DIRECT

10.1.3.0/24 -> C

C:

10.1.1.0/24 -> B

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Example - Anteater (SIGCOMM'11)

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10.1.3.0/24 -> C

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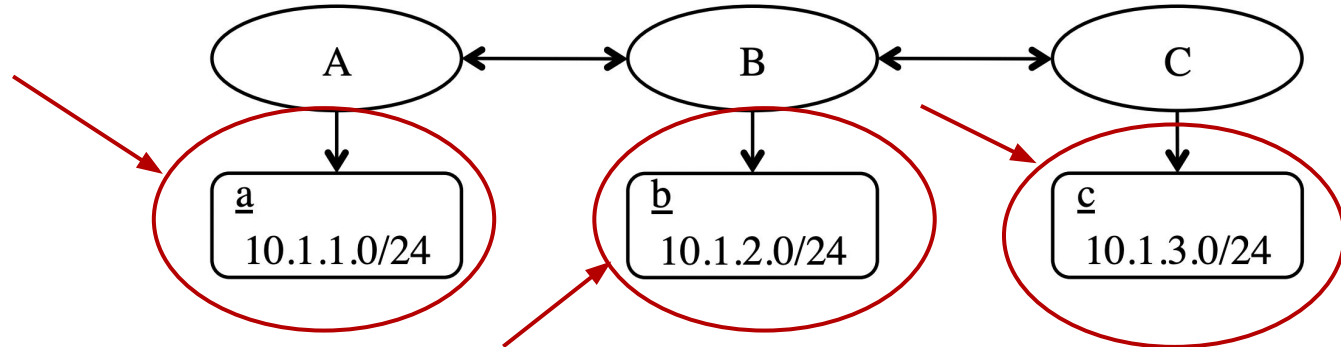
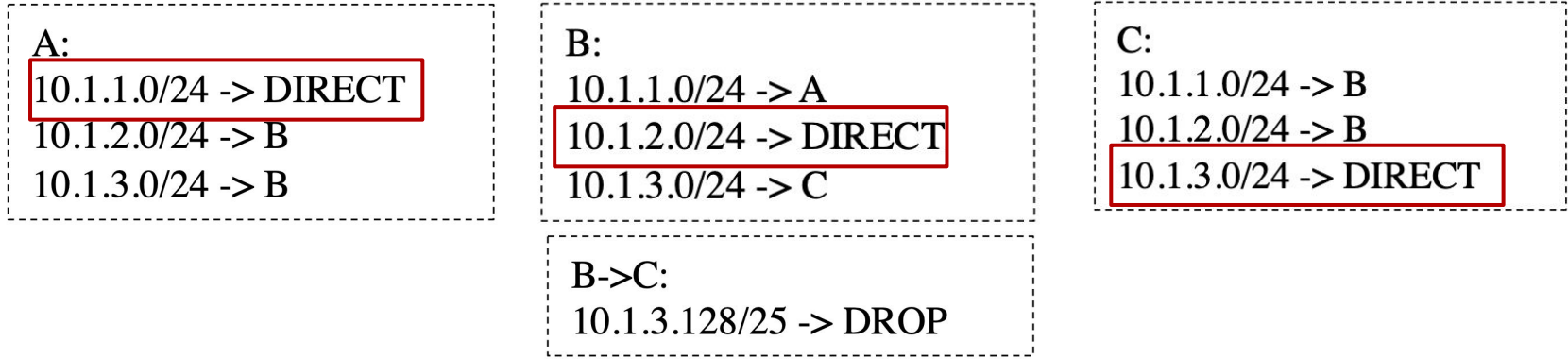
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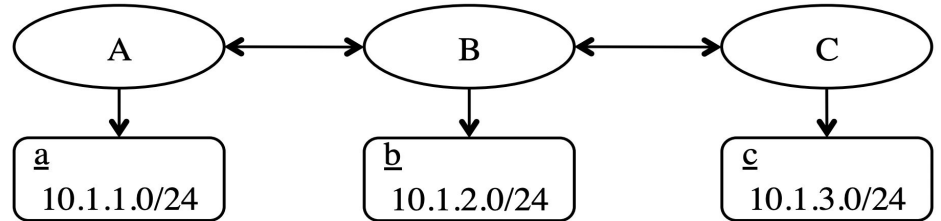
C:
10.1.1.0/24 -> B
10.1.2.0/24 -> B
10.1.3.0/24 -> DIRECT

B->C:
10.1.3.128/25 -> DROP

Model each bit in the packet as a boolean variable.

- The rules only use destination IP, so we only model the 32 bits in the destination IP address.

$P(\mathbf{x}, \mathbf{y})$: boolean formula describing which packets can go from \mathbf{x} to \mathbf{y} .



Example - Ant eater (SIGCOMM'11)

A:
10.1.1.0/24 -> DIRECT
10.1.2.0/24 -> B
10.1.3.0/24 -> B

B:
10.1.1.0/24 -> A
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10.1.3.0/24 -> C

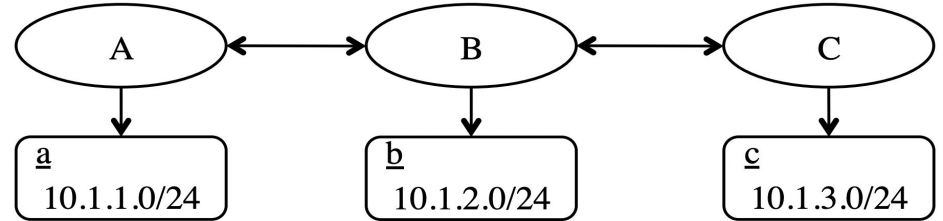
C:
10.1.1.0/24 -> B
10.1.2.0/24 -> B
10.1.3.0/24 -> DIRECT

B->C:
10.1.3.128/25 -> DROP

$P(x, y)$: boolean formula describing which packets can go from x to y .

$P(A, a) = \text{dst ip} =_{24} 10.1.1.0$

$P(A, B) = \text{dst ip} =_{24} 10.1.2.0$
 $\vee \text{dst ip} =_{24} 10.1.3.0$



Example - Anteater (SIGCOMM'11)

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10.1.3.0/24 -> C

C:
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10.1.2.0/24 -> B
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$P(x, y)$: boolean formula describing which packets can go from x to y .

$P(A, a) = \text{dst ip} =_{24} 10.1.1.0$

$P(A, B) = \text{dst ip} =_{24} 10.1.2.0$
 $\vee \text{dst ip} =_{24} 10.1.3.0$

$\text{dst ip} =_w \text{prefix}$

is a shorthand for

$\bigwedge_{32-w \leq i \leq 32} (\text{dst ip}[i] = \text{prefix}[i])$

Example - Ant eater (SIGCOMM'11)

A:
10.1.1.0/24 -> DIRECT
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10.1.3.0/24 -> B

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10.1.1.0/24 -> A
10.1.2.0/24 -> DIRECT
10.1.3.0/24 -> C

C:
10.1.1.0/24 -> B
10.1.2.0/24 -> B
10.1.3.0/24 -> DIRECT

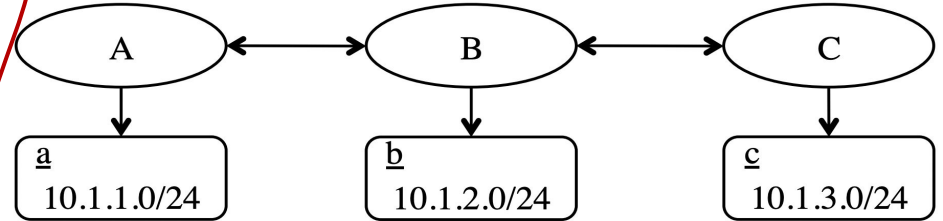
B->C:
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$P(x, y)$: boolean formula describing which packets can go from x to y .

$P(B, A) = \text{dst ip} =_{24} 10.1.1.0$

$P(B, b) = \text{dst ip} =_{24} 10.1.2.0$

$P(B, C) = \text{dst ip} =_{24} 10.1.3.0$
 $\wedge \text{dst ip} \neq_{25} 10.1.3.128$



Example - Anteater (SIGCOMM'11)

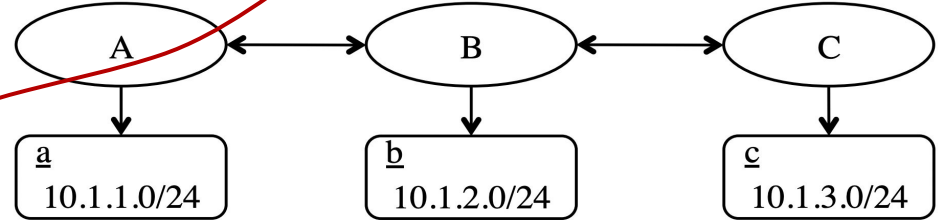
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C:
10.1.1.0/24 -> B
10.1.2.0/24 -> B
10.1.3.0/24 -> DIRECT

B->C:
10.1.3.128/25 -> DROP

$P(x, y)$: boolean formula describing which packets can go from x to y .

$$P(C, B) = \text{dst ip} =_{24} 10.1.1.0 \vee \text{dst ip} =_{24} 10.1.2.0$$
$$P(C, c) = \text{dst ip} =_{24} 10.1.3.0$$


Example - Anteater (SIGCOMM'11)

- Can A reach C?
- Anteater uses a simple graph algorithm to construct the boolean formula that describe all the packets that can reach C from A using $P(x, y)$
- That formula is $P(A, B) \wedge P(B, C)$
- The formula is given to a SAT solver to check if any assignment to the boolean variables, i.e., any destination IP address, exists that can go from A to C
- If no, no packets can reach C from A

Example - Anteater (SIGCOMM'11)

- This was just a simple example
- Anteater shows how to use a similar approach to check for absence of loops and black holes, among other properties.

Reasoning about network forwarding behavior

- Anteater models network behavior as SAT formulas and uses a SAT solver for their analysis.
- Since then, there has been several other proposals for other ways for both modeling and analysis

Reasoning about network forwarding behavior

- Since then, there has been several other proposals for other ways for both modeling and analysis
- Header Space Analysis (HSA) (NSDI'12)
 - models sets of K-bit packets as subspaces in a K-dimensional space
 - uses set operations for analysis
- Veriflow (NSDI'13)
 - uses a trie to find equivalence classes (ECs) of packets
 - models the forwarding behavior of ECs using a forwarding graph
 - analyzes the network behavior using graph algorithms
- There has been a lot more! (see netverify.fun for a survey)

Formal methods in networking

- Data-plane verification
 - Model and analyze the forwarding rules on the data plane
 - Anteater, HSA, Veriflow, ...
- Control-plane verification
 - Model and analyze the control-plane protocols that configure the data plane
- Stateful and programmable data planes

Formal methods in networking

- Analyzing DNS
 - Is there a query under our domain that is sent for resolution to a name server, not under our domain?
- Analyzing performance
 - Is there an input traffic pattern under which the network provides high latency?

Formal methods in networking industry

- Large cloud providers are integrating formal methods into their network operations
 - Microsoft, Amazon, Google, Alibaba, ...
 - "Be sure before shipping – the need for safety in clouds" - Dave Maltz keynote in the netverify'21 workshop organized by Microsoft and Google
- Several startup companies
 - Forward Networks, Veriflow, Intentionet, ...

How does this all relate to programmable networks?

- Automated testing and verification did not start with and is not limited to programmable networks.
- But, programming abstractions for a single device or collection of devices provides extra opportunities.
 - We can reuse so much of the existing knowledge, expertise, and tools for program verification in the formal methods and PL community
 - In our "network" programs, we already have accurate well-defined specifications of network functionality.
 - We can verify the compilers (or their output) to provide end-to-end verified tool chains
 - ...

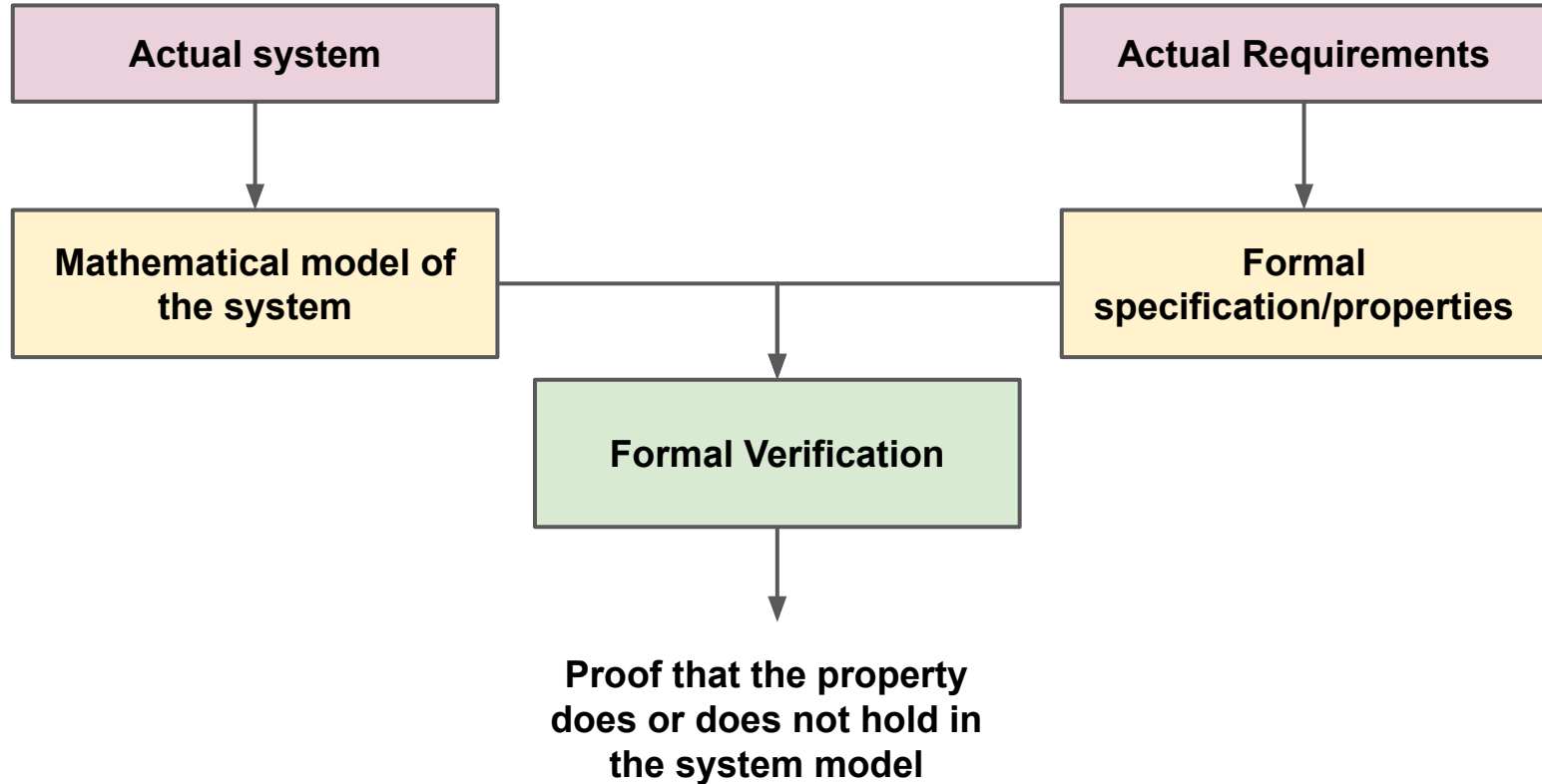
What's next?

- So far, we have convinced ourselves that using formal methods in networking is both essential and possible
- Now, we need to make it usable in a more widespread manner in real-world networks.
- What is missing?

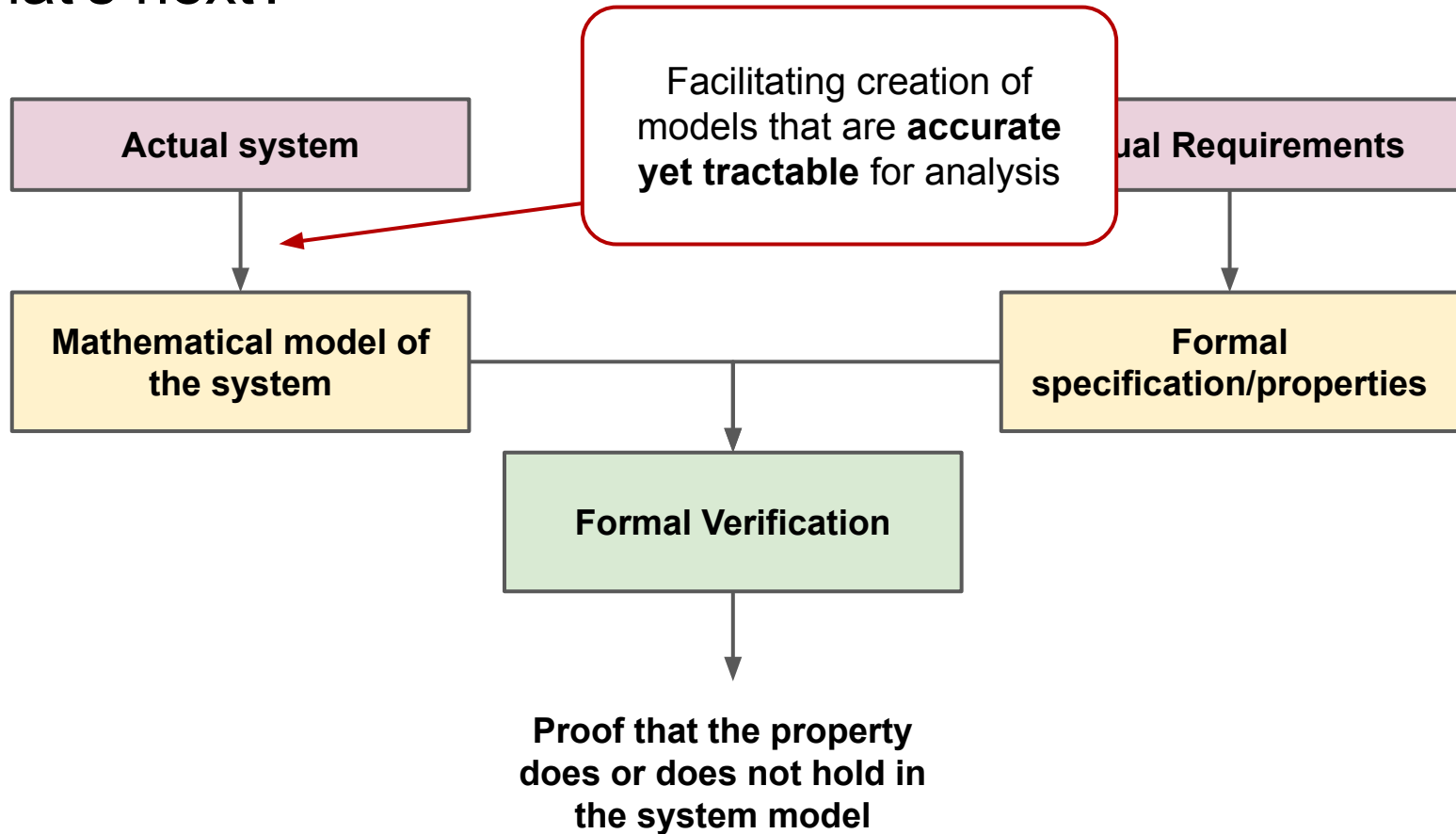
What's next?

- Scale
 - Formal methods tools don't scale well :)
 - There is evidence that they can scale to large network for certain networks and certain properties with lots of optimizations
 - One way forward is "modular" verification, where we verify smaller subsets of the network independently and then combine the results.
 - So, there is hope but also still a long way to go
- Functionalities and properties beyond forwarding
 - network functions, network performance, ...

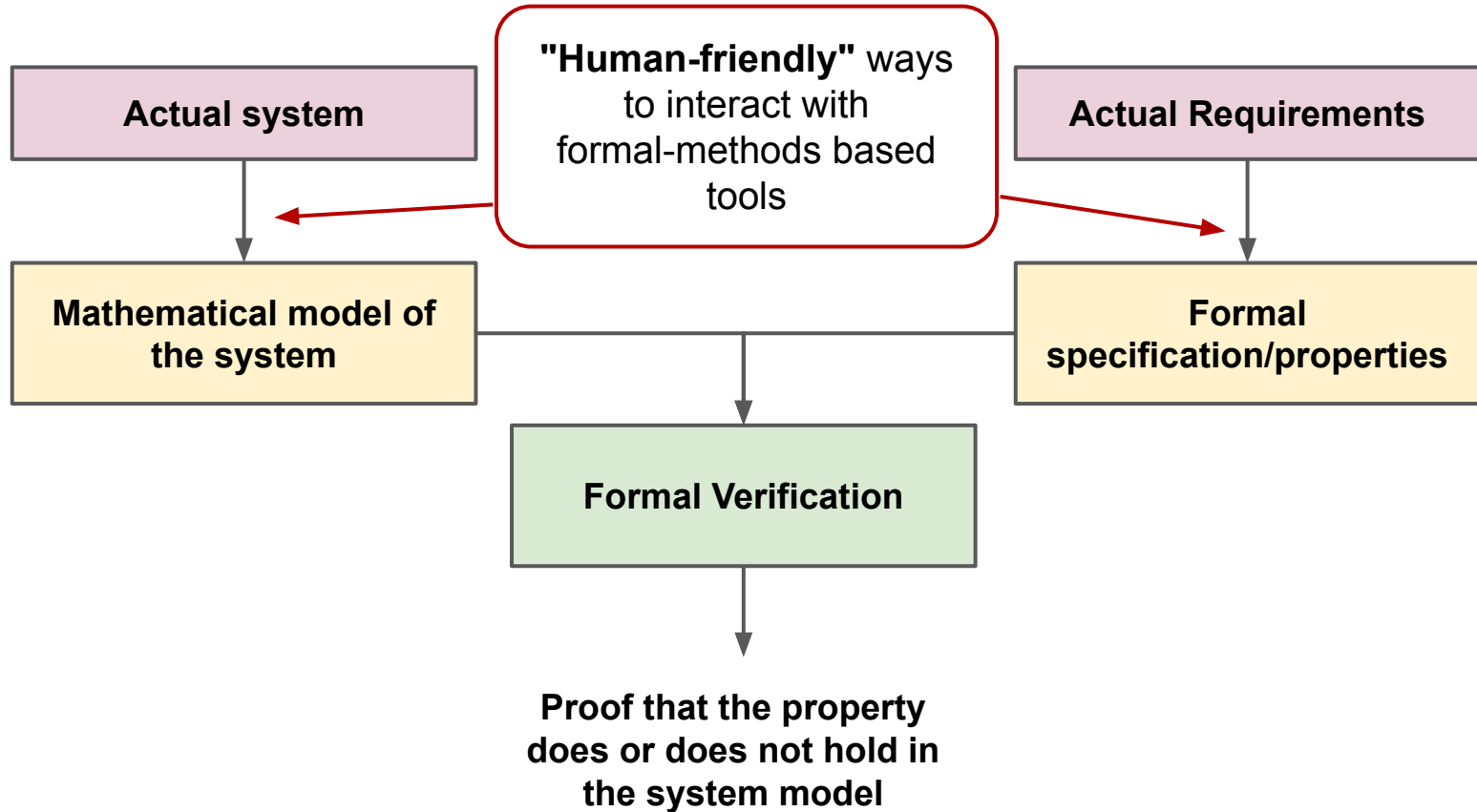
What's next?



What's next?



What's next?



Paper 1: p4v: Practical Verification for Programmable Data Planes

- A tool for verifying properties about P4 programs
 - General safety properties, e.g., avoiding read/writes to invalid headers
 - Program-specific properties specified using assert statements
- Has to work around the fact that the some data-plane rules come from the control plane and are only known at run-time

Paper 2: Validating Datacenters At Scale

- Describes the tools used in Microsoft Azure's network for verifying ACLs and forwarding rules
- To scale, they use domain-specific insights to simplify the analysis
 - Structural properties of the topology
 - Decompose what they want to validate into checks on local devices
 - ...

Additional Resources

- netverify.fun
 - History and survey of verification tools
 - Articles from experts about what's new in the area
- Network verification and synthesis course from University of Washington
- Papers on analyzing DNS and performance, among others